

Available online at www.sciencedirect.com



Journal of Chromatography A, 1011 (2003) 111-123

JOURNAL OF CHROMATOGRAPHY A

www.elsevier.com/locate/chroma

# Development of asymmetrical flow field-flow fractionation-multi angle laser light scattering analysis for molecular mass characterization of cationic potato amylopectin

Seungho Lee<sup>a,1</sup>, Per-Ola Nilsson<sup>b</sup>, Gunilla S. Nilsson<sup>b</sup>, Karl-Gustav Wahlund<sup>a,\*</sup>

<sup>a</sup>Division of Technical Analytical Chemistry, Center for Chemistry and Chemical Engineering, Lund University, P.O. Box 124, S-221 00 Lund, Sweden

<sup>b</sup>Lyckeby Stärkelsen Research and Technology, SE-291 91 Kristianstad, Sweden

Received 24 February 2003; received in revised form 26 June 2003; accepted 27 June 2003

#### Abstract

The goal of this study is to investigate the applicability of asymmetrical flow field-flow fractionation (AsFIFFF)–multi angle laser light scattering (MALLS), and to develop a method for analysis of cationic potato amylopectin (CPAP) having ultrahigh molecular mass (UHM<sub>r</sub>). Use of the aqueous carrier having low salt content (3 mM NaN<sub>3</sub>) resulted in a distortion in AsFIFFF fractograms of CPAP with a general pattern of a sharp rise at the beginning of the elution followed by a long tailing, probably due to combination of attractive and repulsive charge interactions (attractive interaction between CPAP molecules and the channel membrane, and repulsion among cationic CPAP molecules). As the cross flow-rate ( $F_c$ ) increases, the tailing tends to increase, and the repeatability of the AsFIFFF retention data tends to decrease, which is an indication of the presence of the charge interactions. The tailing gradually decreased, and the repeatability of the AsFIFFF retention data increased, as the salt content of the carrier increased. The distortion of the fractogram finally disappeared at  $F_c$  of about 0.2 ml/min and the channel flow-rate ( $F_{out}$ ) of about 1 ml/min with the aqueous carrier having the salt content of 40 mM (3 mM NaN<sub>3</sub>+37 mM NaNO<sub>3</sub>). The weight-average molecular mass ( $M_w$ ) and the z-average radius of gyration ( $\langle r_g \rangle_z$ ) determined by MALLS were 5.2×10<sup>7</sup> and 34×10<sup>1</sup> nm, respectively. With the flow-rate ratio,  $F_c/F_{out}$  kept constant, the degree of the charge interactions (and thus the distortion of fractogram) seems to increase with the cross flow-rate ( $F_c$ ) and with the sample injection mass. AsFIFFF–MALLS was applied for determination of molecular mass distributions (M<sub>r</sub>Ds) and the sizes of CPAPs prepared by various cooking procedures.

© 2003 Published by Elsevier B.V.

*Keywords:* Asymmetrical flow field-flow fractionation; Multi-angle laser light scattering; Molecular weight distribution; Field-flow fractionation; Cationic potato amylopectin; Starch

\*Corresponding author. Tel.: +46-46-222-8316; fax: +46-46-222-4525.

(K.-G. Wahlund).

<sup>1</sup>Present address: Department of Chemistry, Hannam University, Taejon 306-791, South Korea.

## 1. Introduction

Starches are widely used in various industries, and are often modified (or derivatized) in order to expand their applicability and to obtain desired properties for particular applications [1]. To optimize the modi-

 $0021-9673/03/\$ - see \ front \ matter \ @ 2003 \ Published \ by \ Elsevier \ B.V. \ doi:10.1016/S0021-9673(03)01144-0$ 

E-mail address: karl-gustav.wahlund@teknlk.lth.se

fication and the processing (and thus the use) of starch materials, the knowledge of the relationship between the modification or the processing parameters and the properties of the final starch product is required, and thus the chemical and physical properties of the starch materials need to be measured. One of the most important properties of the starch materials is the molecular mass distribution ( $M_rD$ ), as it affects the chemical, physical and rheological properties of the starch material.

Flow field-flow fractionation (FIFFF) is a technique that could be useful for analysis of ultra-large polymer molecules such as the starch materials. FIFFF provides separation of polymers based on the hydrodynamic size (or molecular mass,  $M_r$ ), and some physical properties of the samples can be directly determined from their retention data. Applicability of FIFFF has been shown for analysis of various polymers and colloidal particles, including water-soluble polymers [2–7], humic acids [8], biological polymers [9], liposomes [10], DNAs [11], pigment particles [12], colloidal particles [13,14], ribosome [15], natural organic matters [16,17], wheat proteins [18], aquatic humic colloids [19].

In FIFFF, the diffusion coefficient (and thus the hydrodynamic diameter,  $d_{\rm H}$ ) of the sample can be directly determined from its retention data. In an asymmetrical flow field-flow fractionation (AsFIFFF), the relationship between  $d_{\rm H}$  and the retention time,  $t_{\rm R}$  is given by [15,20]:

$$d_{\rm H} = \frac{2kTV^0}{\pi\eta F_{\rm c} w^2 t^0} \cdot t_{\rm R} \tag{1}$$

where k is the Boltzmann constant, T the absolute temperature (K),  $V^0$  the channel void volume,  $\eta$  the viscosity,  $F_c$  the cross flow-rate, w the channel thickness, and  $t^0$  the channel void time. Eq. (1) is a simplified expression that is applicable only to the cases of relatively high retention. With all experimental parameters fixed constant,  $d_H$  is directly proportional to  $t_R$ .

The application of Eq. (1) is limited to an "ideal" case where there are no charge interactions such as the interaction among the sample molecules or the interaction between the sample and the channel wall.

An ideal condition must be provided in AsFIFFF analysis to obtain accurate results using Eq. (1).

There have already been a few studies on the retention behaviour of positively charged polymers in FIFFF [4,9] but these have been of low to high molecular mass. In this study the aim is to apply FIFFF to polymers of ultra-high molecular mass (UHM), i.e.,  $>10^7$ . FFF analysis of ionic (or charged) species is challenging as it can be complicated by various forms of charge interactions during elution. The charge interactions will result in distortion in the elution profile and inaccurate retention data. The degree of charge interaction may vary with various parameters including the chemical and physical properties of the sample, the type and pH of the carrier, the type and the concentration of salts added in the carrier, and also with the type of the membrane (accumulation wall), etc. It has been shown that the retention of charged molecules or particles is sensitive to the type and the concentration of salts in the carrier, and generally an addition of a certain amount of salt into the carrier (thus increasing the ionic strength) suppresses the charge interactions of charged molecules or particles [7,13,21,22].

Multi angle laser light scattering (MALLS) is a technique that is useful for determination of bulk properties of polymeric samples, such as the average values of the  $M_r$  and the radius of gyration  $(r_g)$  [23]. The on-line coupling of MALLS with FIFFF (FIFFF-MALLS) becomes a powerful tool for determination of the distributions of the  $M_r$  and  $r_q$ . FIFFF provides size (or  $M_r$ )-based separation, and MALLS provides the  $M_{\rm r}$  and  $r_{\rm g}$  of each slice of the FIFFF fractogram, thus yielding distributions of  $M_r$ and  $r_{g}$  of the sample. FIFFF–MALLS has been used for analysis of various samples, including colloidal particles [14], water-soluble polymers [7], polysaccharides [24], celluloses [25], Dextran and tobacco mosaic virus [26], natural colloids [27], κ-carrageenan [28], polyacrylamide [29,30], κ-carrageenan and xanthan [31], and amylopectin [32].

Starch is comprised of two major components, amylopectin and amylose. The goal of this study is to investigate the applicability of AsFIFFF–MALLS for determination of  $M_rD$  and  $r_g$  of cationic potato amylopectin (CPAP), and also to compare CPAPs processed by various cooking procedures.

## 2. Experimental

## 2.1. Asymmetrical flow field-flow fractionation

The AsFIFFF channel was set up as described in previous studies [32,33] with a 130- $\mu$ m-thick polyester spacer and a regenerated cellulose membrane (UF-C10, Hoechst) having an  $M_r$ -cutoff of 10,000. The channel geometry was trapezoidal [34,35] with the tip-to-tip length of 28.5 cm and the breadths at the inlet and the outlet of 2.0 and 0.5 cm, respectively.

The carrier was pure water containing various amounts of salt (NaN<sub>3</sub> and NaNO<sub>3</sub>). For all AsFIFFF experiments, the sample was introduced into the channel using a 20-µl loop injector (Rheodyne, Cotati, CA, USA) by the following procedure. First the inlet flow-rate  $(F_{in})$  was set at 1 ml/min, and the channel flow-outlet was closed. Now all the flow entering the channel exits through the cross flow-outlet. Then the valve on the cross flow-outlet tubing was opened to the atmosphere bypassing the needle valve. This reduces the channel pressure down to about 2~3 bar during the sample introduction and relaxation/focusing period. The sample was introduced by a syringe pump at 0.2 ml/min for 30 s. After the syringe pump was turned off, the sample was allowed to relax and focused for 30 s. After the relaxation and focusing, the inlet flow-rate was adjusted to the desired level and the valve on the cross flow-outlet tubing was returned to its normal elution position, at which point the data collection was started. During elution of the sample, the channel pressure reaches around 6~10 bar, depending upon the flow-rate conditions.

All samples were diluted with the carrier before the injection. Two on-line detectors were used, which were a DAWN-DSP MALLS detector (Wyatt Technology, Santa Barbara, CA, USA) followed by an Optilab DSP interferometric refractive index (RI) detector (Wyatt Technology). Both detectors were equipped with 633 nm lasers. A filter [Millipore Type RA 1.2  $\mu$ m filter put into a high-performance liquid chromatography (HPLC) pre-column filter holder after being cut out by a hole puncher] was placed between the outlet of the channel and the MALLS detector to reduce the noise in light scattering data.

## 2.2. Cationic potato amylopectin

A CPAP sample (called "CPAP") was prepared as a test material for the applicability of AsFIFFF for CPAP analysis. It was 100% potato amylopectin (PAP) cationized by the reaction of PAP with 2,3epoxy propyl trimethyl ammonium chloride. The degree of substitution (DS) was measured to be 0.061. This means that on average there were 6.1 substituents per 100 anhydroglucose units. The DS was calculated as DS = (162N)/(14 - 151N), where N is the mass fraction of nitrogen in the sample, and 162, 151, and 14 are the molecular masses of the anhydroglucose unit, the substituent, and nitrogen, respectively. The samples were carefully washed with 50% ethanol before nitrogen determination according to the Kjeldahl method. A method was developed for dissolution of CPAP in water. First, CPAP was jet-cooked at 120 °C with a flow of 80 1/h without backpressure. No granules were found in the stock solution by optical microscopy. The viscosity of a 1% (w/v) jet-cooked solution of CPAP was approximately 100-200 cP at 50 °C. All other percentage concentrations in this work are also in w/v. The jet-cooked CPAP solution was freeze-dried. A 0.2% stock solution of CPAP was prepared by dissolving the freeze-dried CPAP in water containing 3 mM NaN<sub>2</sub> (0.02%) at 100 °C for 30 min in a Reacti-Therm (Pierce, Rockford, IL, USA) with constant stirring. The stock solution was diluted with carrier at 0.01~0.02% for AsFIFFF analysis. Previously measured dn/dc values for various starch derivatives were in the range between 0.145 and 0.155 ml/g, and a dn/dc value of 0.15 was used for light scattering calculations for all CPAP materials used in this study.

To study the effect of cooking conditions on the MWD of CPAP, two more samples of the CPAP (called "CPAP#1" and "CPAP#2", respectively) were prepared. Each of them was cooked by three different procedures, namely jet-cooking at 130 °C, jet-cooking at 140 °C, and batch-cooking at 95 °C, yielding three samples for each of CPAP#1 and CPAP#2 (six samples in total). For jet-cooking, 187 g of CPAP was slurried into 10 kg of deionized water, and then cooked in a heated continuous cooker ("jet-cooker") at the flow-rate of about

80 1/h. During cooking, the pressures in the cooking zone were 2.4 and 1.7 bar, at the cooking temperatures of 140 and 130 °C, respectively. The viscosities, measured as 1% dry substance by a Brookfield viscometer (spindle 3, 100 rpm, 50 °C), were 111 and 160 cP for the CPAP#1 cooked at 140 and 130 °C, respectively, and 105 and 122 cP for CPAP#2 cooked at 140 and 130 °C, respectively. For batch-cooking, 5.5 g of dry CPAP was weighed in a 1000-ml glass beaker, and then deionized water was added to a total of 550 g. The beaker was placed in a boiling water bath (95 °C) for 30 min. During the batch-cooking, the slurry was stirred at 1000 rpm using a high shear stirrer. The viscosity of the batchcooked CPAP, measured in the same way as above, was 437 cP, which is much higher than those of jet-cooked CPAPs. All preparations were freezedried and stock solutions prepared by dissolution as described above.

#### 3. Results and discussion

### 3.1. Retention behaviour, ionic strength

Fig. 1 shows AsFIFFF elution profiles of CPAP obtained with water containing 3 mM (about 0.02%) NaN<sub>3</sub> as the carrier. The sample injection mass was



Fig. 1. AsFIFFF fractograms of CPAP obtained in water with 3 mM NaN<sub>3</sub>.  $F_c/F_{out}$  was varied with  $F_{in}$  kept constant at about 1.2 ml/min. The sample injection mass was 2.04 µg (20 µl injection of 0.0102% solution).

2.04 µg (20 µl injection of 0.0102% sample solution). The ratio of the cross flow-rate ( $F_c$ ) to the channel flow-rate ( $F_{out}$ ),  $F_c/F_{out}$  was varied while  $F_{in}$  was kept constant at 1.25 ml/min. The void times ( $t^0$ ) were calculated by the AsFIFFF theory [34,36]. All fractograms in Fig. 1 show distorted elution profiles with a general pattern of a sharp rise at the beginning, followed by a long tail. The distortion becomes increasingly serious as  $F_c$  increases. At  $F_c$  of 0.91 ml/min, the tailing was so serious that the elution did not end until the run was terminated at 30 min.

In an ideal situation where charge interactions are absent, the ratio,  $t_{\rm R}/t^0$  is given by [20]:

$$\frac{t_{\rm R}}{t^0} = \frac{w^2}{6DV^0} \cdot F_{\rm c} \tag{2}$$

With all other experimental parameters kept constant, the ratio  $t_{\rm R}/t^0$  of a sample is proportional to the cross flow-rate,  $F_{\rm c}$ .

In Eq. (2), D is the diffusion coefficient of the sample. For many polymers, the diffusion coefficient is inversely dependent on the  $M_r$  [37]. With all the experimental parameters kept constant, AsFIFFF provides a separation based on the diffusion coefficient, and thus a separation based on the  $M_r$ . The retention time increases as D decreases or the  $M_r$  increases.

The ratio,  $t_{\rm R}/t^0$  and  $d_{\rm H}$  calculated for the data shown in Fig. 1 are summarized in Table 1. For each fractogram,  $t_{\rm R}$  was measured at three different positions (the maximum of the early eluting peak, the end of the tailing, and the midpoint between the previous two positions). For the fractogram obtained at  $F_{\rm c} = 0.91$ , only one position was measured at the peak maximum as the end point of the elution was not clear due to tailing.

According to Eq. (2), the ratio,  $t_{\rm R}/t^0$  is expected to increase proportionally with  $F_{\rm c}$  in an ideal condition. And, of course, the hydrodynamic diameter,  $d_{\rm H}$  should remain constant even if the flow-rate changes. In Table 1,  $t_{\rm R}/t^0$  does not show a proportional increase with  $F_{\rm c}$ . The  $t_{\rm R}/t^0$  measured at the peak maximum was even decreased (by 14%) when  $F_{\rm c}$  was increased from 0.12 to 0.56 ml/min. The  $d_{\rm H}$ values measured at all three positions of the fractogram were also decreased when  $F_{\rm c}$  was increased

F <sub>c</sub> (ml/min)	F <sub>out</sub> (ml/min)	$F_{\rm c}/F_{\rm out}$	t <sup>0</sup> (min)	Measured position	t <sub>R</sub> (min)	$t_{\rm R}/t^0$	d <sup>*</sup> <sub>H</sub> (nm)
0.12	1.09	0.11	0.32	Peak max	1.80	5.6	238 (21.2)
				Middle	3.10	9.7	416
				End	4.40	13.8	595
0.56	0.66	0.85	0.41	Peak max	1.96	4.8	43 (2.7)
				Middle	6.30	15.4	142
				End	10.5	25.6	239
0.66	0.56	1.18	0.44	Peak max	2.52	5.7	43 (5.2)
				Middle	8.00	18.2	142
				End	13.5	30.7	240
0.91	0.34	2.68	0.55	Peak max	3.44	6.3	35 (5.0)

Table 1 AsFIFFF retention of CPAP in water with 3 mM  $NaN_3$ 

The sample injection mass was 2.04 µg (20 µl injection of 0.0102% solution).

Numbers in parentheses are standard deviations. \* Calculated by Eq. (1).

from 0.12 to 0.56 ml/min, indicating the sample elutes earlier than they should at higher  $F_c$ . At  $F_c$  higher than 0.56,  $t_R/t^0$  increases with  $F_c$  as theory predicts (although it is not exactly proportional), and  $d_H$  tends to stay nearly constant.

The disagreement with theory discussed above in AsFIFFF retention behaviours of CPAP is probably due to the electrostatic repulsion between the cationic CPAP molecules. As  $F_{\rm c}$  increases, molecules



Fig. 2. AsFIFFF fractograms of CPAP obtained using an aqueous carrier with the total salt content of 20 mM (3 mM NaN<sub>3</sub>+17 mM NaNO<sub>3</sub>).  $F_c/F_{out}$  was varied while  $F_{in}$  was kept constant at about 1.2 ml/min. The sample injection mass was 4.08 µg (20 µl injection of 0.0204% solution).

are pushed closer to the accumulation wall (forming a thinner layer close to the accumulation wall) and move closer to each other. The cationic molecules will then tend to repel each other and move away from the accumulation wall, and will be eluted earlier than they would in the absence of the charge interactions. As  $F_c$  increases further, molecules are pushed even closer to the membrane, and it seems that attractive interactions starts to come into play, causing long tailing as seen in Fig. 1 for  $F_c$  of 0.91 ml/min.

Generally the charge interaction decreases in a medium with higher ionic strengths [13]. Fig. 2 shows AsFIFFF fractograms of CPAP obtained at various flow-rate combinations ( $F_c/F_{out}$ ) using water with the total salt content of 20 mM (3 mM NaN<sub>3</sub> + 17 mM NaNO<sub>3</sub>) as the carrier. The tailing still exists, but overall elution profiles of the fractograms were much improved compared to those in Fig. 1 (where the salt content of the carrier was 3 mM), probably due to reduced charge interactions.

The ratio,  $t_{\rm R}/t^0$  and  $d_{\rm H}$  calculated at the peak maximum of the fractograms shown in Fig. 2 are summarized in the first three rows of Table 2. Overall, the  $t_{\rm R}/t^0$  values (and thus the  $d_{\rm H}$  values) are higher than those measured at the peak maximum of the fractograms shown in Fig. 1 (see Table 1), and this increase in retention is probably due to reduced charge repulsion. As in Table 1,  $t_{\rm R}/t^0$  does not show

		×	3	31	
F <sub>out</sub> (ml/min)	$F_{\rm c}/F_{\rm out}$	t <sup>0</sup> (min)	t <sub>R</sub> (min)	$t_{\rm R}/t^0$	d <sup>*</sup> <sub>H</sub> (nm)
0.81	0.54	0.37	3.19	8.6	101 (12.7)
0.72	0.75	0.39	3.48	8.9	85 (9.6)
0.67	0.88	0.40	4.36	10.9	95 (12.2)
1.36	0.85	0.20	2.86	14.3	64 (10.2)
	<i>F</i> <sub>out</sub> (ml/min) 0.81 0.72 0.67 1.36	$\begin{array}{c c} F_{out} & F_c/F_{out} \\ \hline ml/min \\ \hline 0.81 & 0.54 \\ 0.72 & 0.75 \\ 0.67 & 0.88 \\ 1.36 & 0.85 \\ \hline \end{array}$	$\begin{array}{c cccc} F_{out} & F_c/F_{out} & t^0 & \\ \hline (ml/min) & & & \\ \hline 0.81 & 0.54 & 0.37 & \\ 0.72 & 0.75 & 0.39 & \\ 0.67 & 0.88 & 0.40 & \\ 1.36 & 0.85 & 0.20 & \\ \hline \end{array}$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$F_{out}$ $F_c/F_{out}$ $t^0$ $t_R$ $t_R/t^0$ $0.81$ $0.54$ $0.37$ $3.19$ $8.6$ $0.72$ $0.75$ $0.39$ $3.48$ $8.9$ $0.67$ $0.88$ $0.40$ $4.36$ $10.9$ $1.36$ $0.85$ $0.20$ $2.86$ $14.3$

Table 2 AsFIFFF retention of CPAP in water with the total salt content of 20 mM (3 mM NaN<sub>3</sub>+17 mM NaNO<sub>3</sub>)

The sample injection mass was 2.04 µg (20 µl injection of 0.0102% solution).

Numbers in parentheses are standard deviations. \* Calculated by Eq. (1).



Fig. 3. AsFIFFF fractograms of CPAP obtained using an aqueous carrier with the total salt content of 20 mM (3 mM NaN<sub>3</sub>+17 mM NaNO<sub>3</sub>) at two different inlet flow-rates.  $F_c/F_{out}$  was kept constant at 0.86. The sample injection mass was 4.08 µg (20 µl injection of 0.0204% solution).



Fig. 4. AsFIFFF fractograms of CPAP obtained using an aqueous carrier with the total salt content of 40 mM (3 mM NaN<sub>3</sub>+37 mM NaNO<sub>3</sub>).  $F_c/F_{out}$  was varied while  $F_{in}$  was kept constant at 1.25 ml/min. For both runs, the sample injection mass was 4.08 µg (20 µl injection of 0.0204% solution).

the proportional increase with  $F_{\rm c}$ , which suggests that there still exist charge interactions.

Fig. 3 shows two AsFIFFF fractograms of CPAP obtained using the same carrier as in Fig. 2 at two different inlet flow-rates  $(F_{in})$  while keeping  $F_c/F_{out}$  constant at 0.86. The  $t_R/t^0$  and  $d_H$  values calculated at the peak maximum of the fractograms shown in Fig. 3 are listed in the last two rows of Table 2. According to AsFIFFF theory,  $t_R$  should not change with  $F_{in}$  as long as the flow-rate ratio,  $F_c/F_{out}$ , is kept constant [36]. However, as shown in Fig. 3 and in the last two rows of Table 2,  $t_R$  was decreased from 4.36 to 2.86 min when  $F_{in}$  was increased from 1.26 to 2.52 ml/min, which may be another indication of non-ideality due to the charge interactions.

The total salt content was further increased to 40 mM (3 mM NaN<sub>3</sub>+37 mM NaNO<sub>3</sub>). Fig. 4 shows AsFIFFF fractograms of CPAP obtained at two different flow-rate conditions ( $F_c/F_{out} = 0.21$  and 0.62) while  $F_{in}$  was kept constant at 1.25 ml/min. The fractogram obtained at  $F_c = 0.22$  is almost of a Gaussian profile. However, at higher cross flow-rate ( $F_c = 0.50$  ml/min,  $F_c/F_{out} = 0.67$ ), the fractogram became distorted. This trend of increasing distortion of AsFIFFF fractogram with increasing  $F_c$  was reproducible.

The results shown in Fig. 4 are consistent with the results shown in Fig. 1 in that the distortion in the fractogram increases as the cross flow-rate,  $F_c$ , increases. This trend suggests that  $F_c$  needs to be kept as low as possible to reduce possible charge interactions when analyzing charged molecules using AsFIFFF. However  $F_c$  cannot be lowered too much as the retention (and thus the resolution) is then also lowered [11].

(5  min  Val(3))									
F <sub>c</sub> (ml/min)	F <sub>out</sub> (ml/min)	$F_{\rm c}/F_{\rm out}$	t <sup>0</sup> (min)	t <sub>R</sub> (min)	$t_{\rm R}/t^0$	d <sup>*</sup> <sub>H</sub> (nm)			
0.21	1.04	0.20	0.32	1.91	6.0	143			
0.22	1.03	0.21	0.32	1.92	6.0	136			
Av. 0.22	1.04	0.21	0.32	1.92 (0.01)	6.0	140 (5.0)			
0.48	0.77	0.62	0.38	3.16	8.3	89			
0.51	0.73	0.70	0.39	3.42	8.3	88			
Av. 0.50	0.75	1.32	0.39	3.29 (0.18)	8.3	89 (0.71)			

Table 3 AsFIFFF data of CPAP in water with the total salt content of 40 mM (3 mM NaN<sub>2</sub> + 37 mM NaNO<sub>2</sub>)

The injected sample mass was 4.08 µg (20 µl injection of 0.0204% sample solution).

Numbers in parentheses are standard deviations. \* Calculated by Eq. (1).

The ratio,  $t_{\rm R}/t^0$  and  $d_{\rm H}$  calculated for the peak maximum of the fractograms shown in Fig. 4 are summarized in Table 3. Each run was repeated twice, and all the results are shown with the averages. As mentioned earlier with Eq. (2),  $t_{\rm R}/t^0$  is proportional to  $F_{\rm c}$  under ideal conditions. In Table 3, a 2.2-times increase in  $F_{\rm c}$  (from 0.22 to 0.48 ml/min) resulted in only a 1.4-times increase in  $t_{\rm R}/t^0$  (from 6.0 to 8.3). And the measured  $d_{\rm H}$  was even decreased from 136 to 89 nm. The decrease in measured  $d_{\rm H}$  at higher  $F_{\rm c}$ indicates that the sample was eluted earlier than it should at higher  $F_c$ , probably due to increased charge-repulsion. This result also suggests that  $F_c$  of 0.48 ml/min is too high for an ideal FFF behaviour of the CPAP used in this study. This increase in charge-repulsion may also be a cause for the distortion of the fractogram at  $F_c$  of 0.48 ml/min as shown in Fig. 4.

Based on the results obtained so far,  $F_c$  of 0.2~0.4 ml/min,  $F_{out}$  of 0.8~1 ml/min and the salt content of 40 mM were chosen for AsFIFFF–MALLS analysis of CPAP. At  $F_{out}$  of about 1 ml/min,  $F_c$  of higher than about 0.4 ml/min resulted in too high retention of the sample, causing tailing due to electrostatic interactions. At the same  $F_{out}$ ,  $F_c$  of lower than about 0.2 ml/min resulted in too early elution of the sample.

#### 3.2. Molecular mass distributions

As mentioned earlier, the multi angle light scattering detector, in combination with a concentration detector such as a RI detector, provides the weightaverage molecular mass  $(M_w)$  and the z-average radius of gyration [or the root-mean-square (RMS) radius],  $\langle r_g \rangle_z$ , without the need for a system calibration [23]. In the light scattering detector used in this study, the scattered light intensity is measured at 15 different angles for each slice of the fractograms. In order to obtain  $M_w$  and  $\langle r_g \rangle_z$ , the light scattering signals are plotted against the angle ("Debye plot") for the polynomial curve fitting. The curve fitting must be performed as accurate as possible as  $M_w$  and  $\langle r_g \rangle_z$  are determined from the intercept and the slope of the polynomial curve at the zero angle, respectively.

There are a few parameters that need to be properly chosen for accurate curve fitting; the order of the polynomial function and the angles to be included for curve fitting. As  $M_w$  and  $\langle r_g \rangle_z$  are



Fig. 5. Debye plot (presented by Berry method) of a slice at 1.93 min of the fractogram shown in Fig. 4 at  $F_c = 0.22$  ml/min. Circles are the light scattering data and the dotted line is the result of a third-order polynomial fit.

determined from the intercept and the initial slope of the curve, the higher range of angles may not be needed as long as there are enough many angles in the low range available for extrapolation to zero angle. There are also three different ways of presenting the Debye plot. They are the Debye [23], the Zimm [38], and the Berry method [39]. For low- $M_r$ polymers having  $\langle r_g \rangle_z$  smaller than about 100 nm, the curve fitting is rather simple as the Debye plot is usually linear. However for high- $M_r$  polymers, the Debye plot tends to deviate from the linearity and requires careful examination for accurate curve fitting.

For the fractograms shown in Fig. 4, the Berry method with a third-order polynomial fitting yielded the best results. Fig. 5 shows a Debye plot presented by the Berry method for the slice at the retention time of 1.93 min of the fractogram obtained at  $F_{\rm c} = 0.22$  ml/min. The circles are the light scattering data measured by MALLS at the six different angles of 25.9, 34.8, 42.8, 51.5, 60.0, and 69.3°, respectively, and the dotted line is the result of a third-order polynomial fitting for the six data points. Although there are 15 angles available in total, only the mentioned six were needed for the curve fitting. Moreover, the use of higher angles resulted in rather large imprecision in both  $M_{\rm w}$  and  $\langle r_{\rm g} \rangle_z$  data. The  $M_{\rm w}$ and  $\langle r_{\rm g} \rangle_z$  for this slice are 4.8  $\cdot 10^7$  g/mol and 32  $\cdot 10^1$ nm, respectively. Fig. 6 shows the fractograms shown in Fig. 4 overlaid with the  $M_{w}$  determined by MALLS for each slice. In both cases, the  $M_r$ 



Fig. 6. AsFIFFF fractograms (shown in Fig. 4) and molecular masses of CPAP determined by MALLS.



Fig. 7. Differential and cumulative molecular mass distributions of CPAP obtained for the fractograms shown in Fig. 4.

increases with time, showing the capability of AsFIFFF for  $M_r$ -based separation, as mentioned earlier with Eq. (2). It is noteworthy that the size-resolution was somewhat improved by using higher cross flow-rate ( $F_c = 0.48 \text{ ml/min}$ ), enabling detection of both lower and higher ends of the distribution than at lower cross flow-rate ( $F_c = 0.22 \text{ ml/min}$ ). This is caused by the higher level of retention obtained by higher cross flow-rate as explained with Eq. (2).

Figs. 7 and 8 show  $M_rDs$  and the size distributions obtained by MALLS for the fractograms shown in Fig. 4. In Fig. 7, the two  $M_rDs$  are similar, as they should be, despite the difference in FFF retention



Fig. 8. RMS radius distributions obtained for the fractograms shown in Fig. 4.

behaviour (see Table 3) and the distorted peak profile obtained at  $F_c = 0.48$  ml/min. Here, the improved resolution at the high- $M_r$  end when using the higher crossflow-rate is clearly visible. It is interesting, that even if the elution profile was distorted, the system still separates by molecular mass. In Fig. 8, the size gradually increases with time in both cases, as expected.

The  $M_{\rm w}$  and  $\langle r_{\rm g} \rangle_z$  obtained for the two fractograms shown in Fig. 4 are summarized in Table 4. Despite of the differences in FFF retention data (see Table 3) between two fractograms, both the average molecular mass and the RMS radius are in agreement within one standard deviation. It is noted that, at  $F_{\rm c}$  of 0.50 ml/min, the standard deviations in both  $M_{\rm w}$  and  $\langle r_{\rm g} \rangle_z$ are higher than those at  $F_c$  of 0.22 ml/min. This higher standard deviation at higher  $F_c$  may be related with higher charge interaction, which needs further investigation. It needs to be mentioned here that accurate measurement of radii in this large size range is difficult as it is often subject to relatively large uncertainties and error. The sharp increases in size at the both ends of the plots shown in Fig. 8 may be the results of relatively large uncertainties caused by the low signal-to-noise ratio at the both ends of the RI and MALLS fractograms.

#### 3.3. Sample concentration effects

Fig. 9 shows two AsFIFFF fractograms of CPAP obtained at the same condition ( $F_c = 0.5, F_{out} = 0.75$ ), but with different sample concentrations (0.0204 and 0.0408%). The injection volume was the same at  $20 \,\mu$ l, and thus the injected sample masses were 4.08and 8.16 µg, respectively. As the sample concentration (thus the injection mass) increases, the molecules tend to be eluted earlier and the fractogram

Table 4

Molecular mass and size of CPAP obtained from the light scattering data shown in Fig. 4

F <sub>c</sub> (ml/min)	F <sub>out</sub> (ml/min)	$M_{ m w}$	$\langle r_{\rm g} \rangle_z$ (nm)
0.22	1.04	5.16 (0.44) · 10 <sup>7</sup>	336 (2.1)
0.50	0.75	5.97 (1.64) · 10 <sup>7</sup>	318 (20.6)

The sample injection mass was 4.08 µg (20 µl injection of 0.0204% sample solution).

Numbers in parentheses are standard deviations.

tº(0.39 min) 0.0204% 0 2 4 6 8 Elution time (min) Fig. 9. AsFIFFF fractograms of CPAP obtained in an aqueous

carrier with the total salt content of 40 mM (3 mM NaN<sub>2</sub> + 37 mM) NaNO<sub>3</sub>) at two different sample concentrations (0.0204 and 0.0408%). The injection volume was the same at 20 µl, thus the sample injection mass was 4.08 and 8.16  $\mu$ g, respectively.  $F_c$  and  $F_{\rm out}$  were 0.5 and 0.75 ml/min, respectively.

becomes more distorted, probably due to the increase in charge interactions. The FFF retention data measured for the peak maximum of the two fractograms shown in Fig. 9 are shown in Table 5. As expected, the measured  $d_{\rm H}$  was decreased at higher sample concentration. In Fig. 9, both fractograms seem to come down to the baseline at around 7.8 min. The  $t_{\rm R}/t^0$  and  $d_{\rm H}$  calculated for the elution time of 7.8 min were 20.5 and 220 nm, respectively.  $M_{\rm w}$  and  $\langle r_{s} \rangle_{z}$  determined by MALLS are shown in Table 6. As in Table 4, both  $M_{\rm w}$  and  $\langle r_{\rm g} \rangle_{\rm z}$  did not change significantly (within one standard deviation) with the sample concentration (injection mass), even if the AsFIFFF retention data (and thus  $d_{\rm H}$ ) were different (see Table 5). This proves the advantage of the independent  $M_{\rm r}$  and  $r_{\rm g}$  measurement by MALLS, the results of which are also evident by the rather similar molecular mass distributions shown in Fig. 10.

Table 5 AsFIFFF retention of CPAP shown in Fig. 9

Sample concentration (%)	t <sup>0</sup> (min)	t <sub>R</sub> (min)	$t_{\rm R}/t^0$	d <sup>*</sup> <sub>H</sub> (nm)
0.0204	0.39	3.29	8.3	89 (0.71)
0.0408	0.39	2.52	6.6	69 (3.8)

 $F_{\rm c} = 0.5$ ,  $F_{\rm out} = 0.75$  ml/min, and the carrier was the same as that used in Fig. 4.

\* Calculated by Eq. (1).



Sample concentration (%)	Sample injection mass (µg)	$M_{_{ m W}}$	$\langle r_{g} \rangle_{z}$ (nm)				
0.0204	4.08	$5.97(1.64) \cdot 10^7$	318 (20.6)				
0.0408	8.16	$6.66(1.69) \cdot 10^7$	265 (30.2)				

Table 6 Molecular mass and size of CPAP obtained for the fractograms shown in Fig. 9

 $F_{\rm c} = 0.5$ ,  $F_{\rm out} = 0.75$  ml/min, and the carrier was the same as that used in Fig. 4.

Numbers in parentheses are standard deviations.

#### 3.4. Effects of cooking conditions

All six samples of CPAP#1 and #2 were analyzed by AsFIFFF/MALLS at two different flow-rate conditions ( $F_c/F_{out}$  of 0.2/1 and 0.38/0.84 ml/min). For the batch-cooked samples of CPAP#1 and 2, the channel flow-rate  $(F_{out})$  decreased continuously quickly after the injection, and thus it was not possible to obtain meaningful fractograms. It seemed that the batch-cooked samples still contained starch granules that caused a blockage of the filter that is placed between the AsFIFFF channel and the MALLS. Figs. 11 and 12 show fractograms (RI signals) and  $M_r$  values of jet-cooked CPAPs obtained at  $F_{c}/F_{out}$  of 0.2/1 (Fig. 11) and 0.38/0.84 (Fig. 12), respectively. Again the resolution was improved when  $F_{\rm c}$  was increased from 0.2 to 0.38 ml/min, and a broader range of  $M_r$  values was detected. For all



Fig. 11. AsFIFFF fractograms (RI signal) and molecular masses of jet-cooked CPAPs obtained in the same carrier as in Fig. 9 (40 mM salt content) at  $F_c$  of 0.2 and  $F_{out}$  of 1 ml/min. For better visibility only a fraction of the data points are shown.



Fig. 10. Differential molecular mass distributions obtained by MALLS for the fractograms shown in Fig. 9.



Fig. 12. AsFIFFF fractograms (RI signal) and molecular masses of jet-cooked CPAPs obtained in the same carrier as in Fig. 9 at  $F_c$  of 0.38 and  $F_{out}$  of 0.84 ml/min. For better visibility only a fraction of the data points are shown.

samples, the  $M_r$  increases as the elution time increases, showing the separation by AsFIFFF based on the  $M_r$ .

In both Figs. 11 and 12, the  $M_r$  data of the CPAP#1 jet-cooked at 130 °C are different from those of the others. It spans a higher, but narrower range of  $M_r$ . This deviation may be related with the fact that the CPAP#1 jet-cooked at 130 °C had significantly higher viscosity than the other three samples (see Experimental section) which suggests that it had been much less degraded by the jetcooking procedure. It should be mentioned that it can be difficult to fine-tune the conditions in a jet cooker to reach high reproducibility and this can explain the deviating result. Moreover, for the same elution time, the CPAP#1 jet-cooked at 130 °C has a higher  $M_r$ than the others. This may suggest the CPAP#1 jet-cooked at 130 °C has a different molecular conformation than the others so that the hydrodynamic diameter,  $d_{\rm H}$ , may have a different relationship to the molecular mass, i.e., a more dense structure. More likely however, there is an error in the hydrodynamic diameter, as calculated from the retention time through Eq. (1), which is caused by too early elution. This is clearly noted in Fig. 12 where the CPAP#1 jet-cooked at 130 °C is eluted much earlier than the others despite of its higher  $M_r$ . This is not the expected behaviour in the normal mode of flow FFF, where the retention time increases with  $d_{\rm H}$  (or  $M_{\rm r}$ ) as shown in Eq. (1).

The erroneous  $d_{\rm H}$  is obvious in Table 7 where use of the higher  $F_{\rm c} = 0.38$  ml/min results in about half

ti.E+06 0 CPAP#1, jet-cooked at 130 deg. C 0 CPAP#1, jet-cooked at 140 deg. C 0 CPAP#2, jet-cooked at 130 deg. C 0 CPAP#2, jet-cooked at 140 deg. C 1.E+06 1.E+07 1.E+08 1.E+09 Molecular weight

Fig. 13. Differential molecular mass distributions of jet-cooked CPAPs obtained under the same conditions as Fig. 11.

the observed  $d_{\rm H}$  as compared to at  $F_{\rm c} = 0.2$  ml/min, unlike for the other samples. For the latter there is also a trend to lower observed  $d_{\rm H}$  but much less pronounced and this can be explained by the influence of electrostatic repulsion as discussed above. The deviating behavior of the CPAP#1 jet-cooked at 130 °C could be a result of a mixed mode retention mechanism where, due to the large size, the retention mode is partly that of the steric or lift-hyperlayer mode, which causes a reversal of the elution order in relation to the size. Such effects have been observed before for ultra-large macromolecules such as undegraded, underivatized potato amylopectin [32].

The deviating character of CPAP#1 jet-cooked at 130 °C becomes even clearer in Figs. 13 and 14

Table 7 AsFIFF/MALLS data of jet-cooked CPAPs in water with the total salt content of 40 mM (3 mM NaN<sub>3</sub>+37 mM NaNO<sub>3</sub>)

F <sub>c</sub> (ml/min)	F <sub>out</sub> (ml/min)	Sample	Cooking temperature (°C)	Injection mass (µg)	t <sup>0</sup> (min)	t <sub>R</sub> (min)	$t_{\rm R}/t^0$	d* (nm)	$M_{ m w}$ $(\cdot 10^6)$	$\langle r_g \rangle_z$ (nm)
0.2	1.0	CPAP#1	130 140	7.3 7.5	0.34 0.34	1.42 1.76	4.2 5.2	111 138	120 47	337 265
		CPAP#2	130 140	8.3 7.3	0.33 0.33	1.73 1.75	5.2 5.3	130 131	63 55	231 218
0.38	0.84	CPAP#1	130 140	7.3 7.5	0.36 0.36	1.63 2.65	4.5 7.4	63 103	117 39	324 231
		CPAP#2	130 140	8.3 7.3	0.37 0.37	2.58 3.07	7.0 8.3	91 103	53 49	277 274

\* Calculated by Eq. (1).



Fig. 14. Differential molecular mass distributions of jet-cooked CPAPs obtained under the same conditions as Fig. 12.

where the M<sub>r</sub>Ds are demonstrated based on the data shown in Fig. 11 ( $F_c/F_{out}$  of 0.2/1) and Fig. 12  $(F_{\rm c}/F_{\rm out}$  of 0.38/0.84), respectively. In both Figs. 13 and 14, the CPAP#1 jet-cooked at 130 °C has the highest  $M_r$  and the narrowest  $M_rD$  among all four samples. The M<sub>r</sub>D became narrower at higher cross flow-rate as shown in Fig. 14, as opposed to those of the other samples. For the latter the wider MrD reflects the improvement in size separation resolution obtained by the increased retention level caused by the increased cross flow-rate. The narrower observed apparent M<sub>r</sub>D for the CPAP#1 jet-cooked at 130 °C instead demonstrates a deteriorated size separation resolution which would be the result of the mixedmode retention mechanism discussed above. Then the MALLS detector senses a mixture of different sizes in each measured slice instead of a narrow size range. Further investigation is needed for more detailed discussion on this matter.

All AsFIFFF/MALLS data are summarized in Table 7. At  $F_c/F_{out}$  of 0.2/1 and 0.38/0.84 ml/min, the CPAP#1 jet-cooked at 140 °C has  $M_w$  values of  $4.7 \cdot 10^7$  and  $3.9 \cdot 10^7$ , respectively, which are much lower than those of the same sample cooked at 130 °C ( $1.2 \cdot 10^8$  and  $1.2 \cdot 10^8$ ). This suggests the CPAP#1 was significantly more degraded at 140 °C than at 130 °C. Also the CPAP#1 jet-cooked at 140 °C has the lowest  $M_w$  among all four cooked samples, indicating it has been more degraded than the others.

Unlike the CPAP#1, the CPAP#2 jet-cooked at 130 and 140 °C do not show much difference in  $M_rD$  (see Figs. 13 and 14). At  $F_c/F_{out}$  of 0.2/1, with the cooking temperature lowered by 10 °C,  $M_w$  and  $\langle r_g \rangle_z$  of the CPAP#2 was reduced slightly from  $6.3 \cdot 10^7$  and  $23 \cdot 10^1$  nm down to  $5.6 \cdot 10^7$  and  $22 \cdot 10^1$  nm, respectively. At  $F_c/F_{out}$  of 0.38/0.84 ml/min, they were reduced from  $5.4 \cdot 10^7$  and  $28 \cdot 10^1$  nm down to  $4.9 \cdot 10^7$  and  $27 \cdot 10^1$  nm, respectively. This result indicates, for the CPAP#2, that there is no significant difference in the degree of degradation during the jet-cooking at 130 and 140 °C.

### 4. Conclusion

The results of this study show the capability of AsFIFFF for  $M_r$ -based (or size-based) separation of charged polymers having ultrahigh molecular mass, such as CPAP. When analyzing charged polymers with AsFIFFF, an effort should be made to reach the "ideal" condition, where no charge interactions are present. This study shows one example of such an effort aimed at developing an AsFIFFF method for analysis of CPAP. Results obtained in this study suggest that  $F_c$  of 0.2~0.4 ml/min,  $F_{out}$  of 0.8~1 ml/min, and the salt content of 40 mM are appropriate for AsFIFFF–MALLS analysis of CPAP.

Different approaches may be required for different charged samples as the degree of charge interactions may vary with various chemical and physical properties of the sample (e.g., charge density and  $M_r$ ), the composition and pH of the carrier, the type and the concentration of salts added in the carrier, and also the type of the channel membrane, etc. The behaviour in FIFFF of charged water-soluble polymers been studied previously [4,9,40]. A detailed discussion on the retention behaviour of polyvinylpyridin [40] regarding ionic strength and sample mass load largely confirms the findings for CPAP in the present study. However, polyvinylpyridin has a high charge density (unity charge per monomer residue) whereas CPAP has a much lower charge density (0.061 charges per monomer residue).

In addition to the salt content, the sample concentration (or the sample mass) is another factor that may require careful attention in optimization of AsFIFFF for analysis of charged polymers. It is noted that the sample mass used in this study was lower than about 8  $\mu$ g (20  $\mu$ l injection of about 0.04% sample solution), which is much lower than that usually used in FIFFF experiments. Although it has not been thoroughly investigated in this study, it is believed that the use of low sample mass helps reducing the charge interactions among charged molecules.

It is evident that a study of the  $M_rD$  by AsFIFFF/ MALLS can reveal variations in the effect on molecular degradation caused by the technological treatment of a starch derivative.

# Acknowledgements

This work was financially supported by a grant from the Lyckeby Stärkelsen Research Foundation, from the Centre for Amphiphilic Polymers from Renewable Sources at Lund University, and from the Swedish Natural Science Research Council. This work was also supported by a Korea Research Foundation grant (KRF-2002-013-D00060).

#### References

- B. Raton, in: O.B. Wurzburg (Ed.), Modified Starches: Properties and Uses, CRC Press, Boca Raton, FL, 1987.
- [2] J.C. Giddings, G.-C. Lin, M.N. Myers, J. Liq. Chromatogr. 1 (1978) 1.
- [3] S.L. Brimhall, M.N. Myers, K.D. Caldwell, J.C. Giddings, J. Polym. Sci., Polym. Lett. Ed. 22 (1984) 339.
- [4] M.A. Benincasa, J.C. Giddings, Anal. Chem. 64 (1992) 790.
- [5] J.J. Kirkland, C.H. Dilks Jr., S.W. Rementer, Anal. Chem. 64 (1992) 1296.
- [6] M.-A. Benincasa, K.D. Caldwell, J. Chromatogr. A 925 (2001) 159.
- [7] H. Thielking, W.-M. Kulicke, Anal. Chem. 68 (1996) 1169.
- [8] R. Beckett, Z. Jue, J.C. Giddings, Environ. Sci. Technol. 21 (1987) 289.
- [9] J.C. Giddings, M.A. Benincasa, M.-K. Liu, P. Li, J. Liq. Chromatogr. 15 (1992) 1729.
- [10] M.H. Moon, J.C. Giddings, J. Pharm. Biomed. Anal. 11 (1993) 911.

- [11] M.-K. Liu, J.C. Giddings, Macromolecules 26 (1993) 3576.
- [12] T. Schauer, Part. Part. Syst. Charact. 12 (1995) 284.
- [13] M.H. Moon, Bull. Korean Chem. Soc. 16 (1995) 613.
- [14] H. Thielking, D. Roessner, W.-M. Kulicke, Anal. Chem. 67 (1995) 3229.
- [15] M. Nilsson, S. Birnbaum, K.-G. Wahlund, J. Biochem. Biophys. Methods 33 (1996) 9.
- [16] G. Newcombe, M. Drikas, S. Assemi, R. Beckett, Water Res. 31 (1997) 965.
- [17] C. Pelekani, G. Newcombe, V.L. Snoeyink, C. Hepplewhite, S. Assemi, R. Beckett, Environ. Sci. Technol. 33 (1999) 2807.
- [18] S.G. Stevenson, T. Ueno, K.R. Preston, Anal. Chem. 71 (1999) 8.
- [19] N.M. Thang, H. Geckeis, J.I. Kim, H.P. Beck, Colloids Surfaces A: Physicochem. Eng. Aspects 181 (2001) 289.
- [20] B. Wittgren, K.-G. Wahlund, H. Derand, B. Wesslen, Macromolecules 29 (1996) 268.
- [21] M.E. Hansen, J.C. Giddings, Anal. Chem. 61 (1989) 811.
- [22] B. Wittgren, K.-G. Wahlund, H. Derand, B. Wesslen, Langmuir 12 (1996) 5999.
- [23] P. Wyatt, Anal. Chim. Acta 272 (1993) 1.
- [24] B. Wittgren, K.-G. Wahlund, J. Chromatogr. A 760 (1997) 205.
- [25] B. Wittgren, K.-G. Wahlund, J. Chromatogr. A 791 (1997) 135.
- [26] H. Thielking, W.-M. Kulicke, J. Microcol. Sep. 10 (1998) 51.
- [27] F.v.d. Kammer, U. Forstner, Water Sci. Technol. 37 (1998) 173.
- [28] B. Wittgren, J. Borgstrom, L. Piculell, K.-G. Wahlund, Biopolymers 45 (1998) 85.
- [29] R. Hecker, P.D. Fawell, A. Jefferson, J.B. Farrow, J. Chromatogr. A 837 (1999) 139.
- [30] R. Hecker, P.D. Fawell, A. Jefferson, J.B. Farrow, Sep. Sci. Technol. 35 (2000) 593.
- [31] C. Viebke, P.A. Williams, Food Hydrocolloids 14 (2000) 265.
- [32] M.v. Bruijnsvoort, K.-G. Wahlund, G. Nilsson, W.Th. Kok, J. Chromatogr. A 925 (2001) 171.
- [33] K.-G. Wahlund, in: M.E. Schimpf, K.D. Caldwell, J.C. Giddings (Eds.), Field-Flow Fractionation Handbook, Wiley, New York, 2000, Chapter 18.
- [34] A. Litzen, K.-G. Wahlund, Anal. Chem. 63 (1991) 1001.
- [35] A. Litzen, Anal. Chem. 65 (1993) 461.
- [36] K.-G. Wahlund, J.C. Giddings, Anal. Chem. 59 (1987) 1332.
- [37] C. Tanford, in: Physical Chemistry of Macromolecules, Wiley, New York, 1961, Chapter 6.
- [38] B.J. Zimm, J. Chem. Phys. 16 (1948) 1093.
- [39] G.C. Berry, J. Chem. Phys. 44 (1966) 4550.
- [40] M.A. Benincasa, J.C. Giddings, J. Microcol. Sep. 9 (1997) 479.